

Factor each polynomial completely given below. If a polynomial is not factorable, state this.

1. $3x^2 - 21x$

1. $3x(x-7)$

2. $7x^3 + 5x^2 - 21x - 15$

$$\begin{aligned} &= (7x^3 + 5x^2) + (-21x - 15) \\ &= x^2(7x + 5) + (-3)(7x + 5) \\ &= (x^2 - 3)(7x + 5) \end{aligned}$$

2. $(x^2 - 3)(7x + 5)$

3. $t^2 - 9t + 14$

$$= (t-7)(t-2)$$

3. $(t-7)(t-2)$

Key

4. $6x^2 + 17x + 12$

$$6 \cdot 12 = 72 \quad \text{and} \quad 72 = 8 \cdot 9$$

$$\begin{aligned} \text{so } & 6x^2 + 8x + 9x + 12 \\ &= (6x^2 + 8x) + (9x + 12) \\ &= 2x(3x + 4) + 3(3x + 4) \\ &= (2x + 3)(3x + 4) \end{aligned}$$

4. $(2x + 3)(3x + 4)$

5. $9x^3 - 6x^2 - 24x$

$$= 3x(3x^2 - 2x - 8)$$

$$= 3x(3x + 4)(x - 2)$$

5. $3x(3x + 4)(x - 2)$

foil check

$$(3x + 4)(x - 2)$$

$$= 3x^2 - 6x + 4x - 8$$

$$= 3x^2 - 2x - 8 \quad \checkmark$$